

# Perturbative and Non-perturbative Effects In String Vacua

I. Modern String Theory &  
implications for particle physics –D-branes

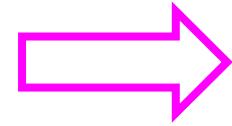
II. Supersymmetric Standard Model  
w/ intersecting D-branes (particle spectrum &couplings)

III. New non-perturbative effects: D-instantons  
Phenomenological implications: Majorana neutrino  
masses,  $\mu$ -parameter, modified Yukawa couplings

R.Blumenhagen, M.C.,T.Weigand, hep-th/0609191 (initiated major activity);  
M. C.,R.Richter,T.Weigand, hep-th/0703028;  
R.Blumenhagen,M.C.,D.Lüst,R.Richter,T.Weigand, arXiv:0707.1871;  
R.Blumenhagen,M.C.,R.Richter,T.Weigand,arXiv:0708.0403.

IV. Conclusions/outlook

**Quest to unify forces of nature**



**Green&Schwarz'84**

**String Theory – most promising candidate**

**as a consistent (finite) quantum theory of strings where  
elementary particles arise as massless excitations of strings.**

**In particular, gravitons - massless excitations of closed strings**

**Quantum gravity for free!**

**Standard Model of elementary particle interactions (strong, weak & electromagnetic) based on Non-Abelian Gauge theory**

$$\mathbf{SU(3)_C \times SU(2)_L \times U(1)_Y}$$

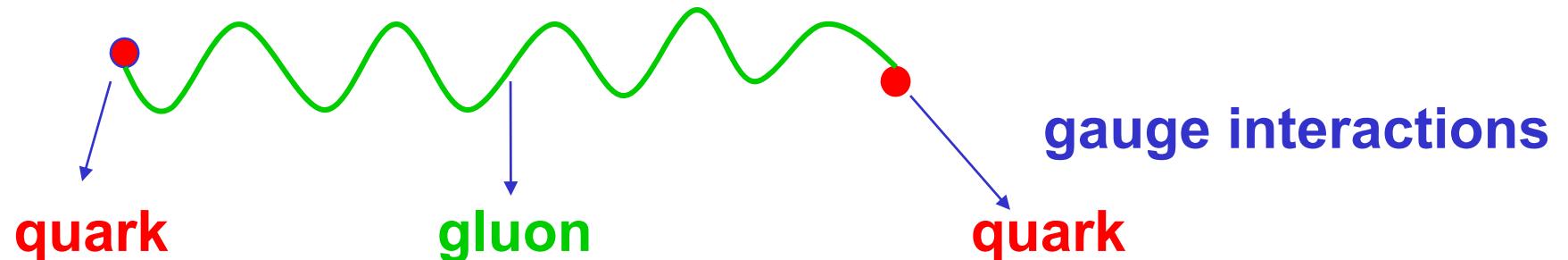
**Force mediated via spin 1-particles: gluons, W-bosons & photon**

**3-families:**

$Q_L \sim ( \underline{3}, \underline{2}, \frac{1}{6} )$  – quarks

$L \sim ( \underline{1}, \underline{2}, -1 )$  – leptons, etc.

chiral  
matter



& Supersymmetry

**Modern String Theory (w/ D-branes) – geometric origin!**

# Perturbative String Theories (small string coupling)

Hull&Townsend'94

Witten'95

## Non-perturbative Unification

11 dimensional supergravity

$g_{\text{IIA}}$ -strong

Phenomenologically promising  
(Penn) major effort in 80-90-ies&05-ies

Type IIA superstring

$g_{\text{IIA}}$ -weak (closed)

Heterotic  $E_8 \times E_8$  string

(hybrid closed)

M-theory

Heterotic SO(32) string

(hybrid closed)

Modern perspective on particle physics

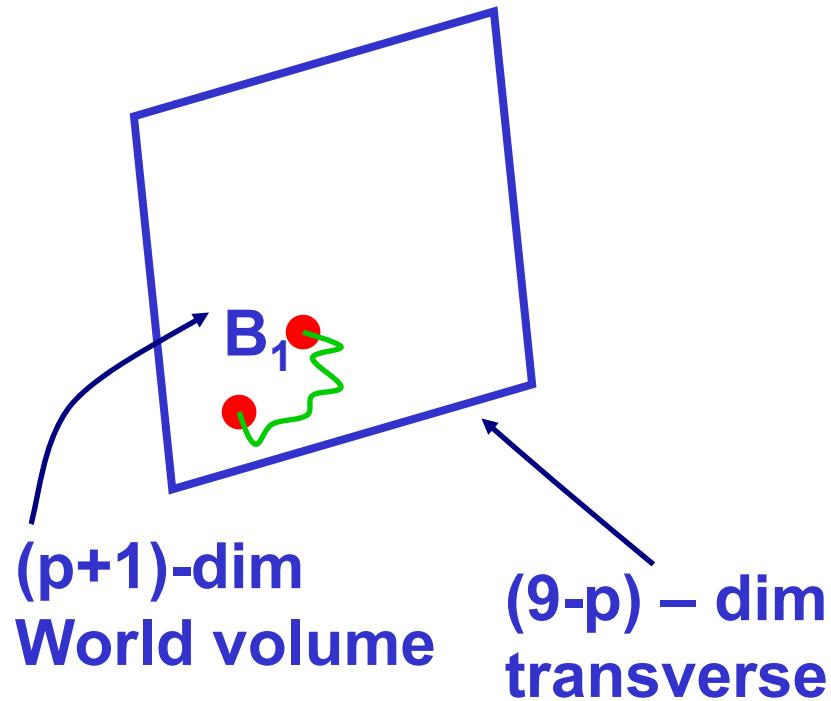
Type I superstring  
(open)

w/advent of  
D-branes

Different String Theories related to each other by Weak-Strong Coupling DUALITY

# D-branes & non-Abelian gauge theory

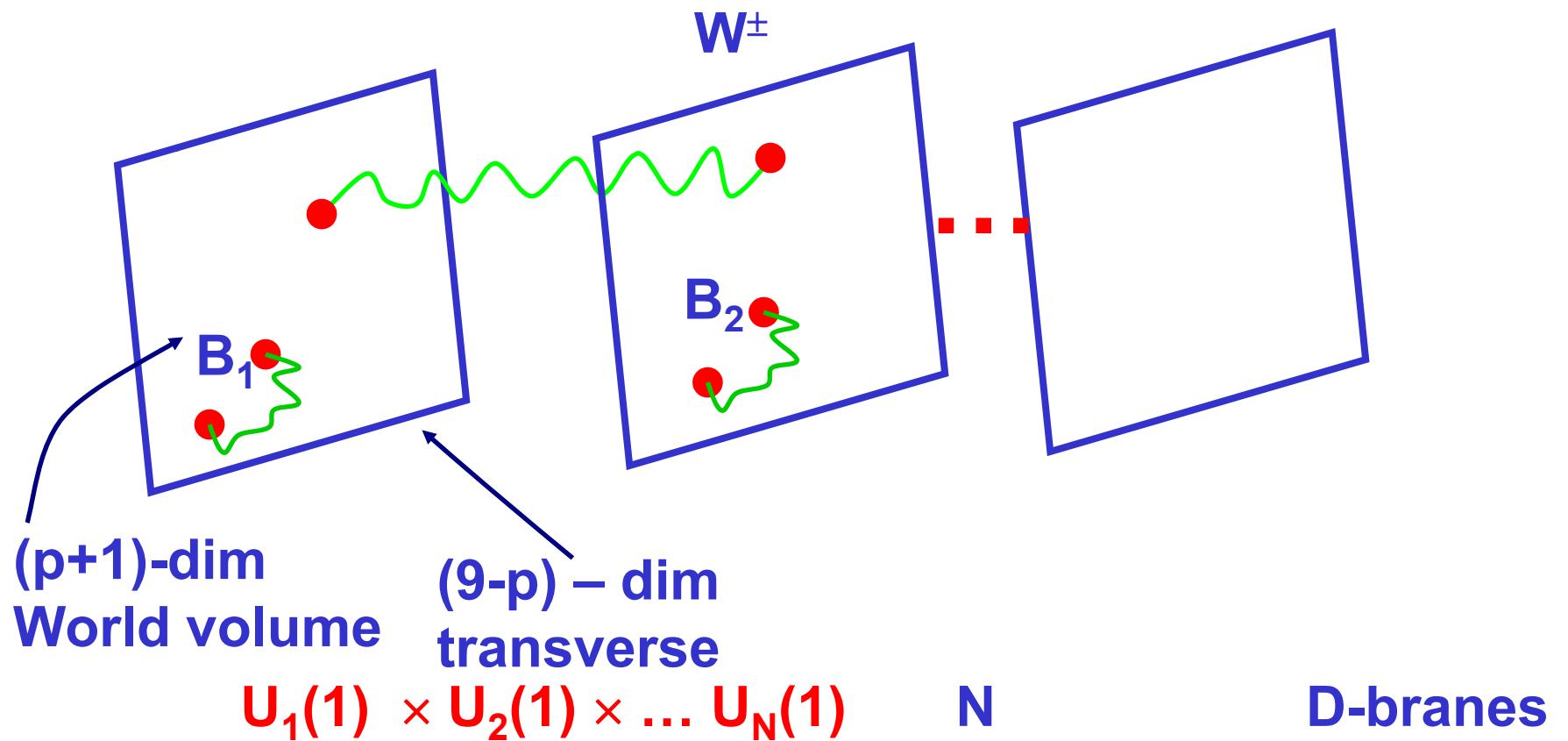
## D p-branes



$B_1 = U(1)$  spin-one particles as massless excitations  
of open strings w/boundaries on a D-brane

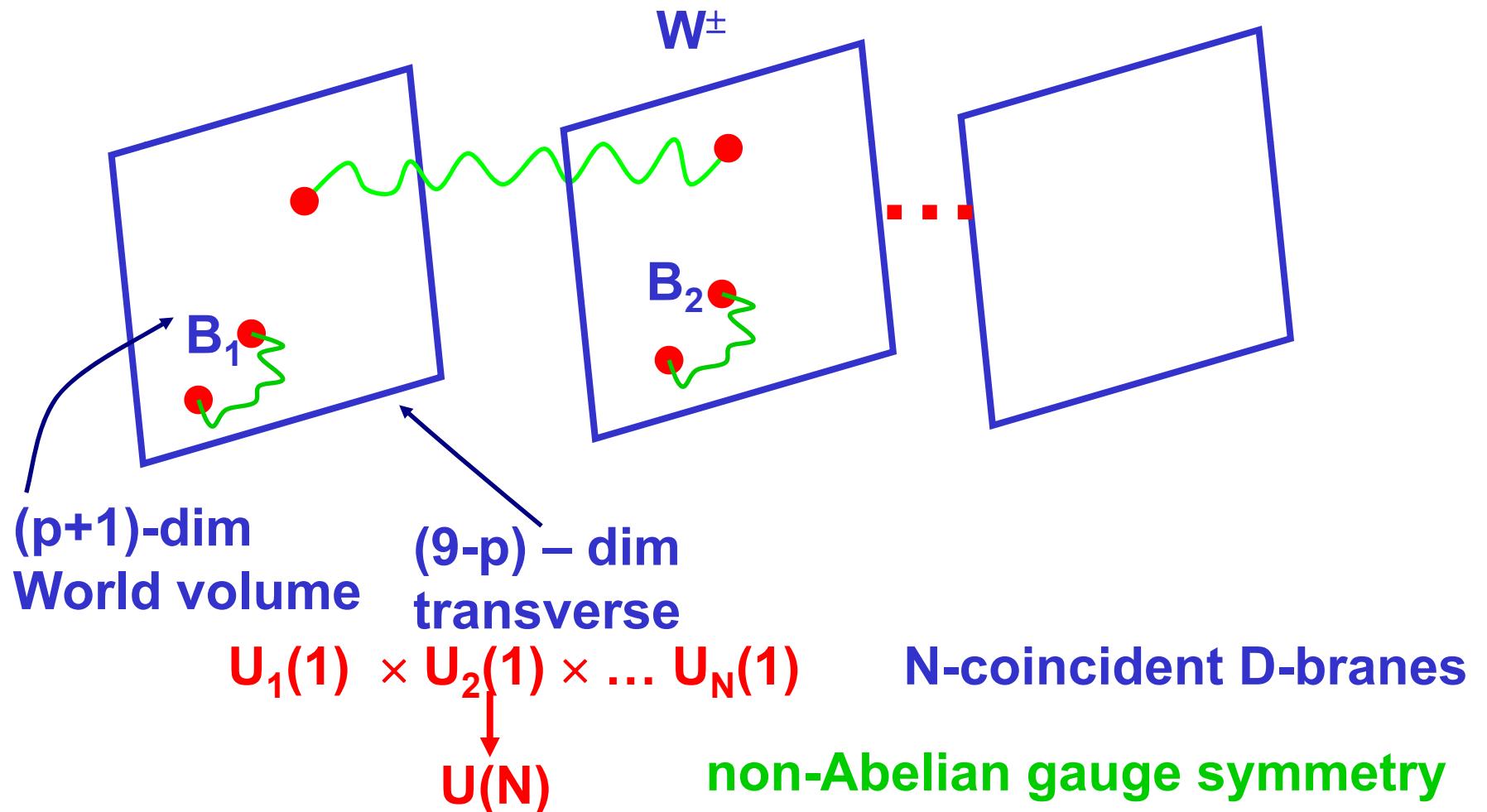
# D-branes & non-Abelian gauge theory

D p-branes



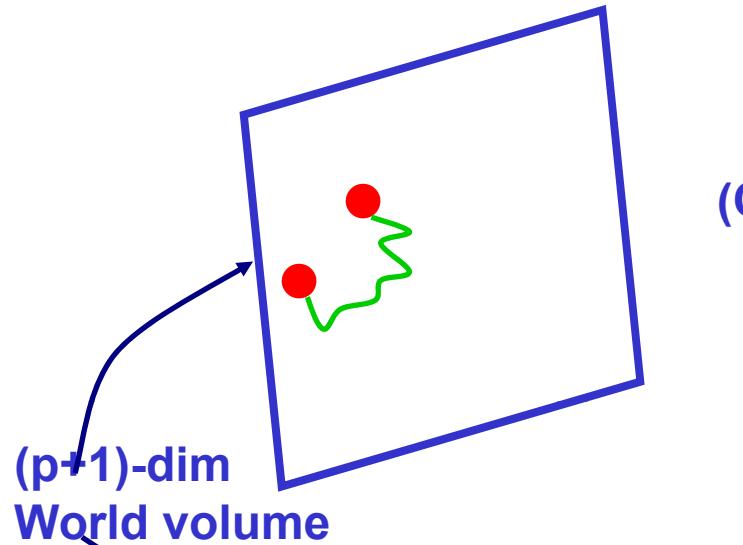
# D-branes & non-Abelian gauge theory

**D p-branes**



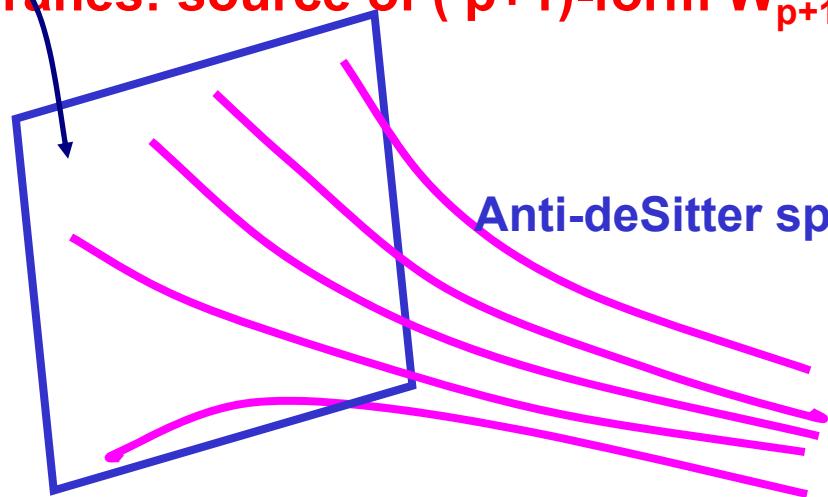
# DIGRESSION-Dual Nature of D-branes

D p-branes: boundaries of open strings



(Conformal) Field Theory

D p-branes: source of  $(p+1)$ -form  $W_{p+1}$  potential & curve space-time



Anti-deSitter space-time (negative cosmol. const.)

Maldacena'97

Anti-deSitter/Conformal Field Theory Correspondence AdS/CFT

Related?  
Yes!

## DIGRESSION: Gravitational role of branes

**Black Holes in string theory**

First constructions suitable for microscopic counting (w/ Youm'95, w/Tseytlin'95,.. Kallosh et al.'93-present...)

Microscopic properties Strominger&Vafa'96, ... w/Tseytlin '95-'96, w/Larsen'97-'00....

**Brane World** Randall&Sundrum'99  
[related -first supergravity domain walls w/ Griffies&Rey'92,...  
w/Soleng'94-'96 (review) ]



**Source for ``Gravity Fluxes''**

Can fix the shape of compactified space-

...Giddings,Kachru & Polchinski'01.., KKLT'03... w/Li&Liu'04...

**Stabilization of Moduli (no time!)**

## **FIELD THEORY SIDE of D-branes (as boundaries of open strings)**

**(i) non-Abelian gauge symmetry**

**N-coincident D-branes**       **U(N)**

**(ii) Appearance of matter**

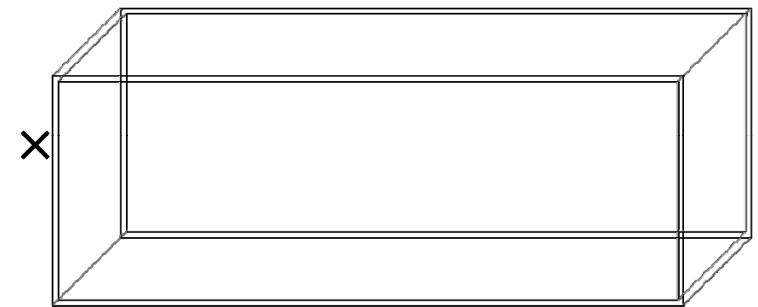
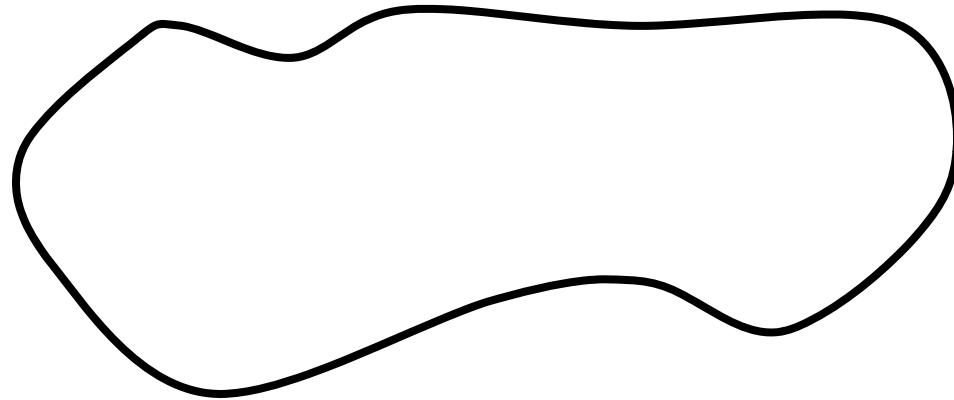
 **turn to compactification**

# Compactification

D=9+1 —————→ D=3+1



X<sub>6</sub>-special space (Calabi-Yau) × M<sub>(1,3)</sub>-flat



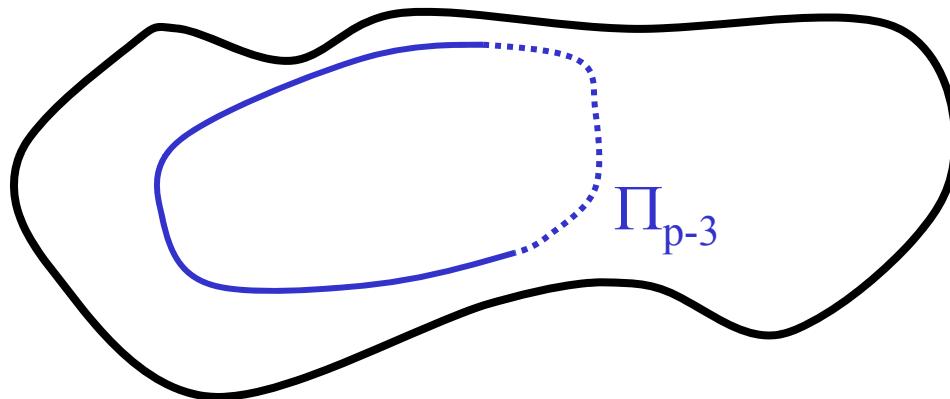
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# Compactification

D=9+1 —————→ D=3+1



$X_6$ -special space (Calabi-Yau)  $\times M_{(1,3)}$ -flat



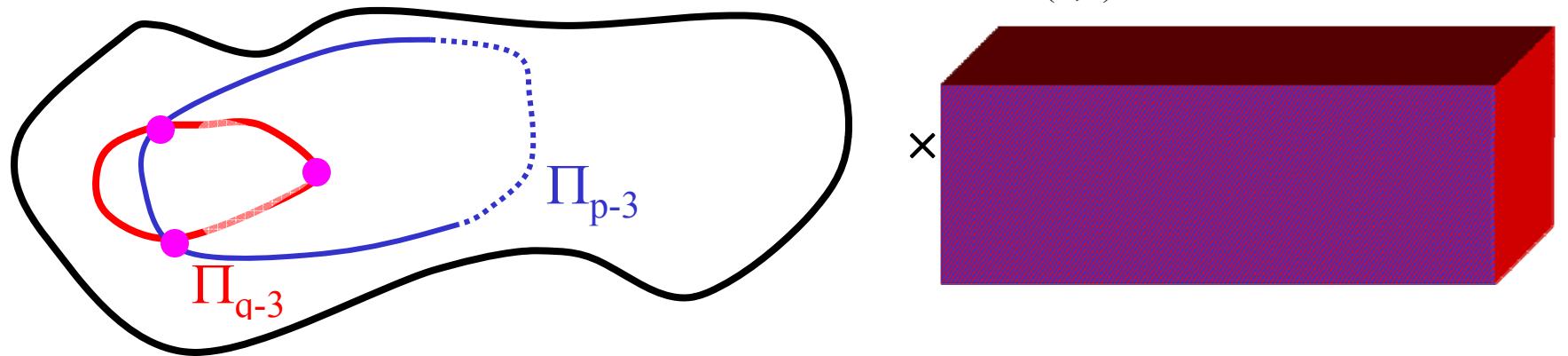
**D p-branes – extend in p+1 dimensions:  
3+1-our world  $M_{(3,1)}$  ;(p-3)-wrap  $\Pi_{p-3}$  cycles of  $X_6$**

# Compactification

D=9+1 —————→ D=3+1



$X_6$ -special space (Calabi-Yau)  $\times M_{(1,3)}$ -flat



D p-branes – extend in p+1 dimensions:

3+1-our world  $M_{(3,1)}$ ; (p-3)-wrap  $\Pi_{p-3}$  cycles of  $X_6$

D q-branes – extend in q+1 dimensions:

3+1-our world  $M_{(3,1)}$ ; (q-3)-wrap  $\Pi_{q-3}$  cycles of  $X_6$

Penn efforts, early '00: D-branes at singularities & Wilson lines  
... w/Wang & Plümacher '00; w/Wang & Uranga '01...

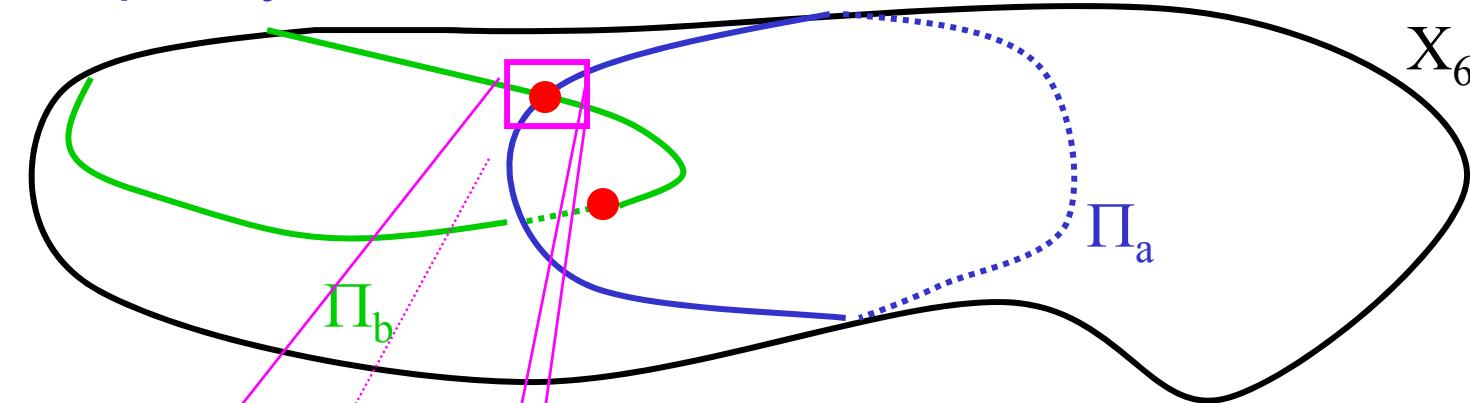
$$\begin{aligned}\Pi_{q-3} \cap \Pi_{p-3} \\ \Pi_{q-3} \subset \Pi_{p-3}\end{aligned}$$



Rich  
structure

# Intersecting D6-branes

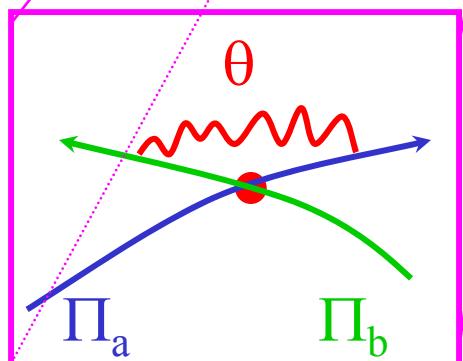
wrap 3-cycles  $\Pi$



In internal space intersect at points:

**Number of intersections  $[\Pi_a] \circ [\Pi_b]$  - topological number**

**Geometric origin of family replications!**



Berkooz, Douglas & Leigh '96

**At each intersection-massless string excitation-  
spin  $\frac{1}{2}$  field  $\psi$  - matter candidate  
Geometric origin of matter!**

# Engineering of Standard Model

$N_a$ - D6-branes wrapping  $\Pi_a$

$N_b$ - D6-branes wrapping  $\Pi_b$

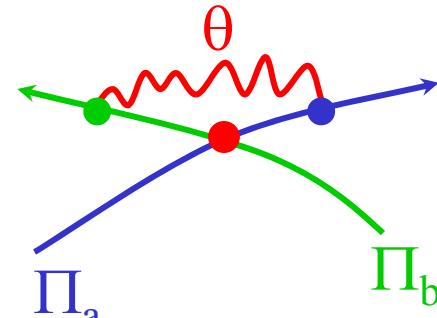
$$U(N_a) \times U(N_b)$$

$\Psi \sim (N_a, \bar{N}_b) - [\Pi_a]^\circ [\Pi_b]$  – number of families

$$N_a = 3, N_b = 2, [\Pi_a]^\circ [\Pi_b] = 3$$

$$U(3)_C \times U(2)_L$$

$\Psi \sim (3, 2)$  - 3 copies of left-handed quarks



Global consistency conditions (D6-brane charge conserv. in internal space)

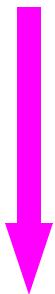
& supersymmetry conditions (constraining!) - technical (no time!)



Building Blocks of Supersymmetric Standard Model

## Explicit Constructions

Special six-dimensional internal space (special Calabi-Yau) :  
compact flat w/isolated singularities



Torus  $T^6$  modded out by discrete symmetry  $(Z_N \times Z_M)$



Orbifold  $T^6/(Z_N \times Z_M)$

[Toy example  $T^2/Z_2$ ]

String theory can be quantized exactly employing  
conformal field theory techniques Dixon et al'85; M.C.,Dixon'85; M.C.'86-'87

## Explicit constructions(CFT-techniques):

Toroidal Orbifolds:  $T^6/\mathbb{Z}_N \times \mathbb{Z}_M$  geometric phase

- Large (infinite) classes of non-supersymmetric Standard Models [Berlin/Munich group'00-'01], [Madrid group'00-'01]
- First three-family supersymmetric Standard Model on  $\mathbb{Z}_2 \times \mathbb{Z}_2$  orbifold [M.C.,Shiu,Uranga '01]

- Majority of supersymmetric models on  $\mathbb{Z}_2 \times \mathbb{Z}_2$ 
  - i. **Semi-realistic constructions** (including  $SU(5)$  GUT's)
    - Systematic searches [Penn group '03-'05] ...
    - Rigid cycles [Blumenhagen, M.C., Marchesano, Shiu '05] ... Coisotropic D8-branes [Font, Marchesano, Ibáñez '06], Further models [Texas A&M group '05-'07], etc.
  - ii. **Coupling calculations**
    - Yukawa couplings [Cremades, Ibàñez, Marchesano '03], [M.C., Papadimitriou '03 (full CFT calculation)] ...
    - Kähler potential [Lüst, Mayr, Richter, Stieberger '04] ...
    - One-loop corrections [Lüst, Stieberger '03], [Abel, Owen '03] ...
  - iii. **Counting (landscape)** [Munich group '05], [Douglas, Taylor '06], ...
- **Other Orbifolds:**
  - [Blumenhagen et al. '03], [Honecker '03] ... brane recombination
  - [Honecker, Ott '05], [Bailin, Love, arXiv:0705.0646 [hep-th]] MSSM, but Yukawas?
- **RCFT models** (non-geometric phase)–large classes of semi-realistic models
  - [Dijkstra, Huiszoon, Schellekens '04] [Anastasopoulos, Dijkstra, Kiritsis, Schellekens '05]

## Three-family SM model w/ $SU(2)_L \times SU(2)_R$ directly ( $Z_2 \times Z_2$ orbifold)

$$\ell^i \equiv 2m^i$$

III	$[U(4)_C \times SU(2)_L \times SU(2)_R]_{observable} \times [U(2)^* \times Sp(8)]_{hidden}$								
stack	$N$	$(n^1, l^1) \times (n^2, l^2) \times (n^3, l^3)$	$n_{\square\square}$	$n_{\square\Box}$	$b$	$c$	$d$	$d'$	2
$a$	8	$(1, 0) \times (1, 3) \times (1, -3)$	0	0	3	-3	0	0	0
$b$	2	$(0, 1) \times (1, 0) \times (0, -2)$	0	0	-	0	-6	6	0
$c$	2	$(0, 1) \times (0, -1) \times (2, 0)$	0	0	-	-	-6	6	0
$d$	4	$(2, -1) \times (1, 3) \times (1, 3)$	$\chi_1 = 24\chi_3/(4 - 9\chi_3^2)$						
2	8	$(1, 0) \times (0, -1) \times (0, 2)$	$\chi_2 = \frac{1}{2}\chi_3, \beta_2^g = -5$						

non-zero  
 Intersections  
 w/hidden sector  
 chiral exotics

wrapping nos. of SM

Cremades, Ibáñez & Marchesano'02

Embedding in  $Z_2 \times Z_2$  orbifold-allows for consistent construction  
 w/ Langacker, Li & Liu, hep-th/0407178

\*\*"hidden sector" (unitary) branes - necessary for global consistency  
 (D-brane charge conservation)

## Four-family Standard Model

Table 2: D6-brane configurations and intersection numbers for the four-family Standard-like model. In the table,  $\chi_i$  is the complex modulus for the  $i$ -th torus, and  $\beta_i^g$  is the beta function for the  $i$ -th  $Sp$  group from the  $i$ -th stack of branes.

$$\ell^i \equiv m^i$$

I	$[U(4)_C \times Sp(8)_L \times Sp(8)_R]_{observed} \times [U(4) \times Sp(8) \times Sp(8)]_{hidden}$									
stack	$N$	$(n^1, l^1) \times (n^2, l^2) \times (n^3, l^3)$	$n \square$	$n \square$	$b$	$c$	$d$	$d'$	1	2
$a$	8	$(1, 0) \times (1, 1) \times (1, -1)$	0	0	1	-1	0	0	0	0
$b$	8	$(0, 1) \times (1, 0) \times (0, -1)$	0	0	-	0	0	0	0	0
$c$	8	$(0, 1) \times (0, -1) \times (1, 0)$	0	0	-	-	0	0	0	0
$d$	8	$(0, 1) \times (1, -1) \times (1, -1)$	0	0	-	-	-	0	-1	1
1	8	$(1, 0) \times (1, 0) \times (1, 0)$	$\chi_2 = \chi_3 = 1$							
2	8	$(1, 0) \times (0, -1) \times (0, 1)$	$\beta_1^g = \beta_2^g = -4$							

no inter-section w/ hidden sector

no chiral exotics!

$Sp(8)_L \times Sp(8)_R$  1-Higgs (8,8), one-family confining hidden sector

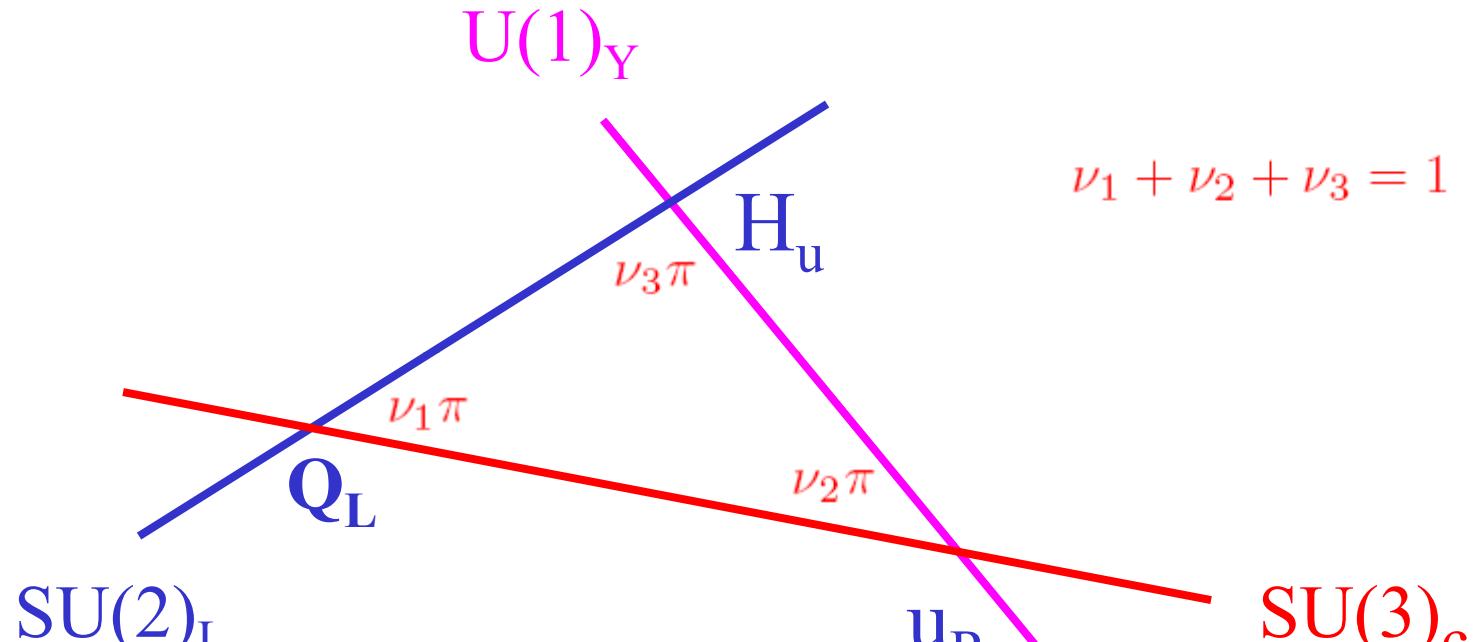
brane splitting

$U(2)_L \times U(2)_R$  16- Higgs (2,2), four-families

brane splitting

# Yukawa Couplings

Intersections in internal space (schematic on  $i^{\text{th}}$ -two-torus)



w/Papadimitriou'03

(Conformal Field Theory Techniques)

$$Y = (2\pi)^{\frac{3}{2}} g_{st} \prod_{i=1}^3 \left[ \frac{\Gamma(1 - \nu_1^i) \Gamma(1 - \nu_2^i) \Gamma(1 - \nu_3^i)}{\Gamma(\nu_1^i) \Gamma(\nu_2^i) \Gamma(\nu_3^i)} \right]^{\frac{1}{4}} \sum_I \exp\left(-\frac{A_I^1 + A_I^2 + A_I^3}{2\pi\alpha'}\right)$$

Geometric!

quantum part

classical part  $A_I^i$  -triangle areas on  $i^{\text{th}}$  two-torus lattice  
Cremades, Ibáñez, Marchesano'03

## Status

- $\mathcal{O}(100)$  toroidal orbifold models (geometric phase) with semi-realistic features
    - typically suffer from chiral exotics
    - problems with realistic Yukawa couplings
    - moduli stabilization issues
- “The devil is in the details”  
though further progress and more promising models are being constructed
- Rational Conformal Field Theory constructions-promising:
    - models without chiral exotics
    - couplings can in principle be calculated, but hard & hierarchy?
    - non-geometric phase-modul stabilization?

## Specific coupling issues

- Neutrino masses – Dirac and of order of charged sector masses

Majorana neutrino masses – absent

- $\mu$ -parameter – typically absent
- SU(5) GUT models – absent  $10\bar{10}5_H$ -couplings

Perturbative absence of all such couplings due to violation of ``anomalous'' U(1)

→ non-perturbative effects due to D-instantons  
**(non-perturbative violation of ``anomalous'' U(1))**

# Anomalous U(1) & Anomaly Cancellation

gauge group  $\prod_a U(N_a) = \prod_a SU(N_a) \times U(1)_a$

in general:  $U(1)_a$  is anomalous

anomaly cancelled by 4D Green-Schwarz mechanism,  
mediated by Chern-Simons couplings,  
arising from Wess-Zumino D-brane action:

$$S_{WZ} = \sum_a N_a \mu_6 \int_{\mathbb{R}^{1,3} \times \Pi_a} e^{tr F_a} \sum_p C_{2p+1}$$

abelian gauge potential becomes massive and anomalous  
 $U(1)_a$  survives as a global perturbative symmetry

In addition, RR  $C_{2p+1}$  forms  
transform under anomalous U(1)

More later

## Prior work... New focus on new D-instanton corrections to charged matter:

### Related work (contemporary with hep-th/0609191)

[Haack,Krefl,Lüst, VanProeyen, Zagermann, hep-th/0609211]

Field theory instantons

[Ibáñez, Uranga, hep-th/0609213] - also emphasis on charged (open sector)

superpotential coupling corrections

Type IIA stringy instantons

[Florea,Kachru,McGreevy,Saulina, hep-th/0610003] Type IIB stringy instantons

### "New generation" of papers (contemporary with hep-th/07003028)

[Abel, Goodsell, hep-th/0612110]

[Akerblom, Blumenhagen, Lüst, Plauschinn, Schmidt-Sommerfield, hep-th/0612132]

[Bianchi, Kiritis, hep-th/0702015],

[Bianchi, Fucito, Morales arXiv:0704.0784[hep-th]]

[Argurio, Bertolini, Ferretti, Lerda, Petersson aeXiv:0704.0262[hep-th]]

[Ibáñez, Schellekens, Uranga, arXiv:0704.1079[hep-th]] extensive RCFT search  
for global models

[Akerblom, Blumenhagen, Lüst, Schmidt-Sommerfeld, arXiv:0705.2366[hep-th]]

one-loop & holomorphic coupling corrections

[Antusch, Ibáñez, T.Macri, arXiv:0706.2132 [hep-ph]] phenomenological study  
of neutrino masses

:

w/ Ralph Blumenhagen & Timo Weigand, hep-th/0609191  
w/Robert Richter & Timo Weigand, hep-th/0603191

## Why non-perturbative (D-INSTANTON) effects?

[affect open string sector-charged matter]

a) Stability of models - drastic

b) May generate perturbatively absent couplings  
w/hierarchy, exponentially suppressed by  $1/g_{\text{string}}$

:

### Phenomenological implications:

a) May generate Majorana neutrino masses in the scale range  
 $10^{11} \text{ GeV} < M_m < 10^{15} \text{ GeV}$  → Realization of seesaw mechanism

b) May generate hierarchically small O(1TeV)  $\mu$ -parameter  
c) May generate the desired Yukawa couplings in SU(5) GUT's

:

## Instantons–Heuristics

Probe for non-pert. terms by computing suitable amplitudes in D-instanton background.

Euclidean  $Dp$ -brane wrapping internal  $(p+1)$ -cycle

→ for Type IIA relevant objects are Euclidean  $D2$ -branes (E2-branes), wrapping three-cycles  $\equiv$

Rules:

- Instanton sector corresponds to local minimum of (full) string action

→  $E2$ -brane volume minimizing

- Integrate over zero modes localized on  $E2$

→ All fermionic zero modes have to appear for relevant instanton induced couplings exactly once

Focus: induced superpotential terms involving charged matter fields  $\Phi_i$

$$W_{np} \propto e^{-S_{E2}} = \exp \left[ \frac{2\pi}{\ell_s^3} \left( -\frac{1}{g_s} \int_{\Xi} \Re(\Omega_3) + i \int_{\Xi} C_3 \right) \right]$$

exponential not gauge invariant under  $U(1)_a$ !

$$e^{-S_{E2}} \rightarrow e^{i Q_a(E2) \Lambda_a} e^{-S_{E2}}: Q_a(E2) = \frac{\ell_s^3}{2\pi} N_a \Xi \circ (\Pi_a - \Pi'_a)$$

CS-coupling induces gauging of global axionic shift symmetry

under  $U(1)_a$  gauge transformation the RR-form  $C_3$ ,  
KK-reduced on 3-cycle  $\tilde{\Pi}$ , transforms as

$$\begin{aligned} A_a &\longrightarrow A_a + d\Lambda_a \\ \int_{\tilde{\Pi}} C^{(3)} &\longrightarrow \int_{\tilde{\Pi}} C^{(3)} + Q_a(\tilde{\Pi}) \Lambda_a \end{aligned}$$

Consequence:

If  $Q_a(E2) \neq 0$  for some  $a$ , no terms  $W = e^{-S_{E2}}$  possible but:

$$W = \prod_i \Phi_i e^{-S_{E2}} \quad \text{with} \quad \sum_i Q(\Phi_i) + Q_a(E2) = 0 \quad \forall a$$

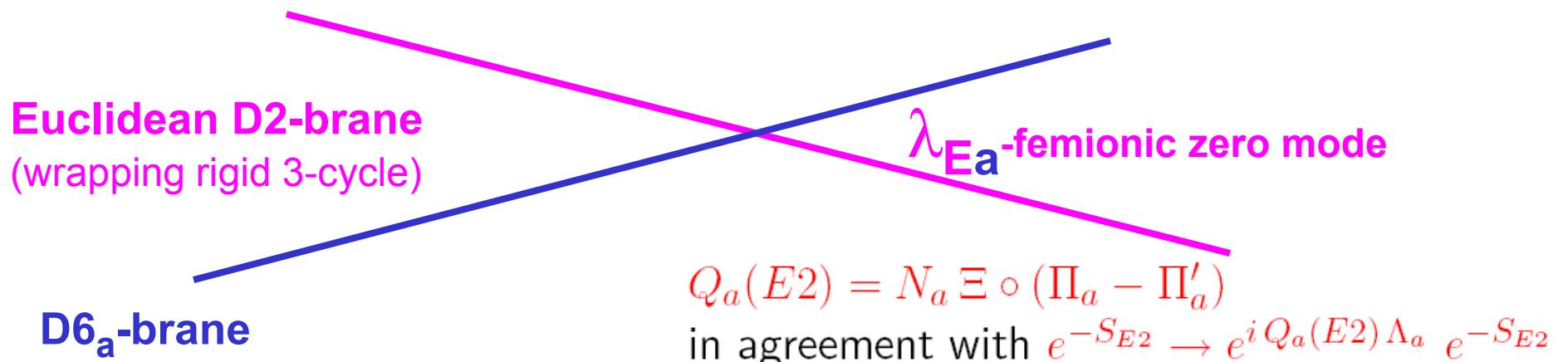
**is possible!**

[non-perturbative breakdown of global  $U(1)$  symmetry]

→ This selection rule explained in terms of fermionic zero modes:

## Constraints on Zero Fermionic Modes:

- I. 3-cycle wrapped by instanton: RIGID & invariant under orientifold projection
- II. Zero modes (strings between  $E2$  and  $D6_a$ ):
  - Localized at the each intersection of  $E2$  and  $D6_a$  branes:
  - One single fermionic zero mode  $\lambda_a$



zero modes	Reps.	number
$\lambda_{a,I}$	$(-1_E, \square_a)$	$I = 1, \dots, [\Xi \cap \Pi_a]^+$
$\bar{\lambda}_{a,I}$	$(1_E, \bar{\square}_a)$	$I = 1, \dots, [\Xi \cap \Pi_a]^-$
$\lambda_{a',I}$	$(-1_E, \bar{\square}_a)$	$I = 1, \dots, [\Xi \cap \Pi'_a]^+$
$\bar{\lambda}_{a',I}$	$(1_E, \square_a)$	$I = 1, \dots, [\Xi \cap \Pi'_a]^-$

Ralph Blumenhagen, M. C., Timo Weigand, hep-th/0609191

**Develop CFT INSTANTON CALCULUS to determine  
non-perturbatively induced superpotential  
couplings quantitatively**

**no time, but c.f. R. Blumenhagen's talk**

## Phenomenological Implications:

### Effects on Superpotential Matter Couplings

One can generate perturbatively forbidden matter couplings:

I. Majorana masses for right-handed neutrinos

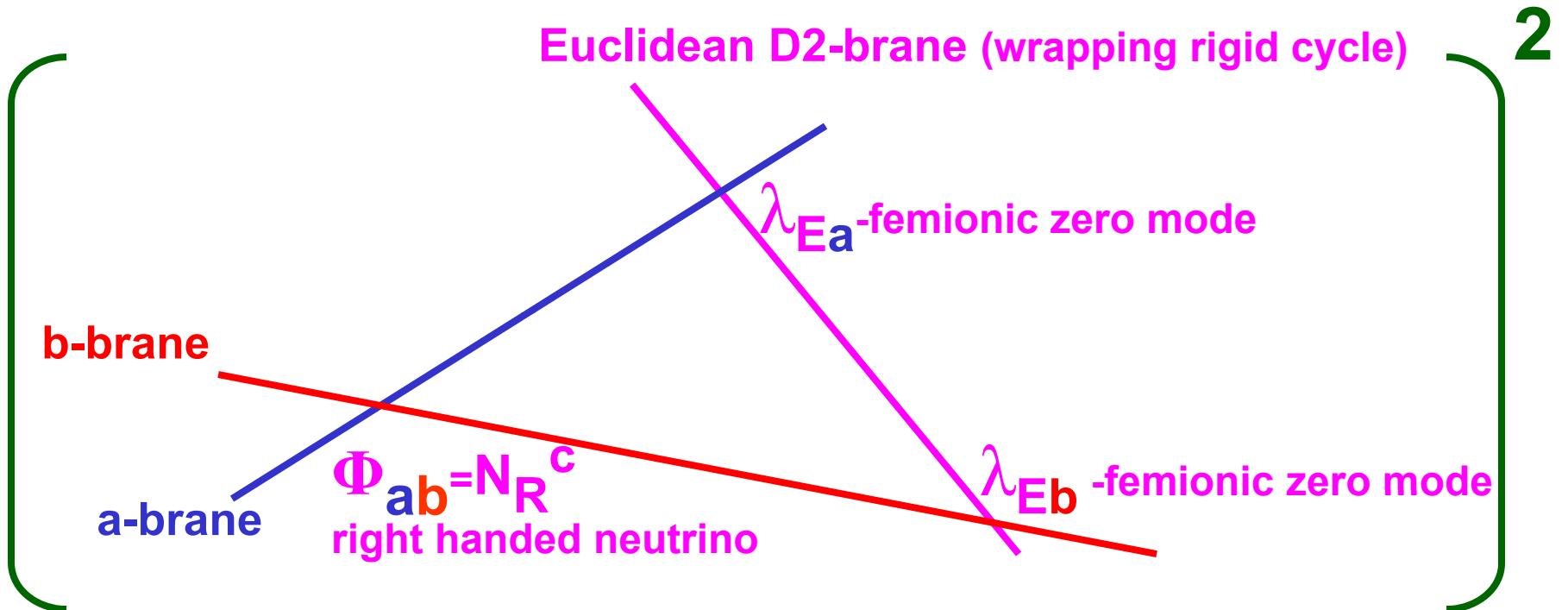
→ Neutrino Dirac masses  $W_H = H^+ L_L (N_R)^c$  typically present, and of order of charged sector masses

Majorana mass  $W_m = M_m (N_R)^c (N_R)^c$  perturbatively forbidden

Note,  $N_R^c$  -Standard Model singlets, typically charged under additional anomalous  $U(1)_a \times U(1)_b$ , say as  $(1, -1)$ .

# Majorana Neutrino Masses:

D2-instanton wraps [2+1 (Euclidean time)]=3-cycle  $[\Pi_{E_2}]$



Non-zero non-perturbative coupling:  $M_m N_R^c N_R^c$

D2-instanton w/  $[\Pi_{SM}]^\circ [\Pi_{E_2}] = 0$ ,  $[\Pi_a]^\circ [\Pi_{E_2}] = 2$  &  $[\Pi_b]^\circ [\Pi_{E_2}] = -2$

→ fermionic zero modes appear precisely ONCE and thus  $M_m$  non-zero

Geometric!

→ Non-pert. Majorana coupling:

$$W_m = M_m (N_R)^c (N_R)^c \text{ with } M_m = x M_s e^{-\frac{2\pi}{\ell_s^3 g_s} \text{Vol}_{E2}}$$

$$\text{Use } \frac{1}{\alpha_{\text{GUT}}} = \frac{1}{\ell_s^3 g_s} \text{Vol}_{D6} \rightarrow M_m = x M_s e^{-\frac{2\pi}{\alpha_{\text{GUT}}} \frac{\text{Vol}_{E2}}{\text{Vol}_{D6}}}$$

For seesaw mechanism need  $10^{11} \text{GeV} < M_m < 10^{15} \text{GeV}$

Possible within natural regime for

$$0.4 \cdot R_{D6} > R_{E2} > 0.2 \cdot R_{D6} \text{ (assume } x = \mathcal{O}(1)).$$

# Concrete realizations on $T^6/\mathbb{Z}_2 \times \mathbb{Z}'_2$

[M. C., Robert Richter, Timo Weigand, hep-th/0703028]

Aim:

- Provide example of model with rigid  $E2$ -brane and suitable zero mode structure → highly constraining
- Realize correct suppression scale for Majorana masses
- Exemplify CFT computation → determine  $x$  exactly

Construct supersymmetric 3-stack GUT model:

$N_c = 5$ : SU(5)-GUT stack       $N_a = N_b = 1$

sector	representation	matter
$(c, c')$	Antisym	<b>10</b>
$(c, a)$	$(\bar{c}, a)$	<b>5</b>
$(c, b)$	$(c, \bar{b})$	<b>5<sub>H</sub></b>
$(a, b)$	$(\bar{a}, b)$	$N_R^c$

with correct zero mode structure

$$[\Pi_{E2} \cap \Pi_a]^+ = 2, \quad [\Pi_{E2} \cap \Pi_b]^- = 2, \quad [\Pi_{E2} \cap \Pi_c]^\pm = 0$$

Constraining!

Extensive search merely leads to local set-up with 4 families of **10** and 32  $N_R^c$

**Result:**  $\langle \nu^A \nu^B \rangle_{E2i} = \frac{2\pi}{g_s} \mathcal{V}_{E2} \vec{v}^T \mathcal{M} \vec{v} (2\pi)^4 \delta^4(k^A + k^B)$

$$\mathcal{M} = x M_s e^{-\frac{2\pi}{\alpha_{\text{GUT}}} \frac{8}{57}} \begin{pmatrix} A_i & 0 & B_i & 0 \\ 0 & C_i & 0 & D_i \\ B_i & 0 & E_i & 0 \\ 0 & D_i & 0 & F_i \end{pmatrix} A_i B_i \dots \sim \exp(-A/\alpha')$$

$x =$

$$\frac{(4\pi)^{3/2} \pi^2}{16} \left[ \Gamma_{1-\theta_{ab}^1, 1-\theta_{E2a}^1, 1+\theta_{E2b}^1} \prod_{I=2}^3 \Gamma_{-\theta_{ab}^I, -\theta_{E2a}^I, 1+\theta_{E2b}^I} \right]^{\frac{1}{2}} e^{Z'}$$

$e^{Z'}$  —one-loop contribution [Akerblom et al. arXiv:0705.236 [he-th]]

Overall exponential suppression scale fixed by SUSY:

$$\frac{\text{Vol}_{E2}}{\text{Vol}_{\Pi_c}} = \left( \prod_I \frac{(n_{E2}^I)^2 + (\tilde{m}_{E2}^I)^2 U_I^2}{(n_c^I)^2 + (\tilde{m}_c^I)^2 U_I^2} \right)^{1/2} = \frac{8}{57}$$

- Sum up contributions from all 64 factorizable E2-instantons, taking leading contribution (smallest triangle)  
→  $M_M \simeq 10^{10} \text{GeV}$   
for triangles of order string scale (as required)
- Together with perturbative Dirac masses of  $\mathcal{O}(\text{TeV})$  (due to Yukawa couplings of the type  $\bar{\mathbf{5}} \mathbf{5}_H \mathbf{1}$ )  
→ Can engineer small neutrino masses of  $\mathcal{O}(1\text{eV})$  via see-saw mechanism.

## II. Further applications:

- $\mu$ -term  $\mu H^+ H^-$  forbidden perturbatively  
→ can well be generated by  $E2$ -instantons!  
→ appropriate volume ratio may yield  $\mu \simeq \mathcal{O}(\text{TeV})$
- R-parity violating couplings in the MSSM can be induced (constrains!)
- GUT  $SU(5)$  suffer from absence of pert. Yukawa couplings  $10\ 10\ 5_H$ , where 10 from (a,a')-intersection  
Can be generated by  $E2$ -instantons!

R. Blumenhagen, M.C., D.Lüst, R. Richter, T. Weigand, arXiv:0707.1871

→ Opens doors for phenomenological studies of (flipped)  $SU(5)$

no more time, but c.f. R. Blumenhagen's talk

# Summary/Outlook

- (a) Major progress: development of techniques **for consistent constructions on orbifolds w/intersecting D-branes**  
(primarily on toroidal orbifolds)
- (b) Sizable number of semi-realistic models; **systematic searches** (not-fully realistic-typically some chiral exotic matter)
- (c) Coupling calculation developed –Yukawa couplings, etc.
- (d) **Non-perturbative (D-instanton) effects:**  
**New hierarchical couplings:**  
**Majorana neutrino masses → seesaw mechanism realized within a local model**  
 **$\mu$ -parameter, SU(5) GUT Yukawa couplings,...**

**Challenge: search for global models with realistic features realizing D-instanton effects!**

## Foresee further progress:

- (a) **DEVELOPMENT of TECHNIQUES!** →generalize constructions to general Calabi Yau spaces
- (b) Further study of non-perturbative effects:  
**Vacuum de/re-stabilization:**SUSY breaking/open-string moduli stabilization  
**Effects of additional zero modes:** non-rigid cycles, instanton cycle recombination, flux effects, etc.  
R.Blumenhagen,M.C. R.Richter,T. Weigand, arXiv:0708.0403  
[flux effects, c.f., also Tripathi,Trivedi '05, Kallosh, Kashani-Poor,Tomasiello'05]
- (c) Quantitatively improve **realistic model** constructions, including further progress on globally consistent models with desired non-perturbative effects

**FULLY REALISTIC CONSTRUCTIONS  
particle spectrum & interactions?**

**NOT THERE YET, BUT GETTING BETTER AT IT**

**EFFORTS PRESENTED PLAYING KEY ROLE**